

GCSE MARKING SCHEME

AUTUMN 2023

GCSE
MATHEMATICS – NUMERACY
UNIT 1 – INTERMEDIATE TIER
3310U30-1

INTRODUCTION

This marking scheme was used by WJEC for the 2023 examination. It was finalised after detailed discussion at examiners' conferences by all the examiners involved in the assessment. The conference was held shortly after the paper was taken so that reference could be made to the full range of candidates' responses, with photocopied scripts forming the basis of discussion. The aim of the conference was to ensure that the marking scheme was interpreted and applied in the same way by all examiners.

It is hoped that this information will be of assistance to centres but it is recognised at the same time that, without the benefit of participation in the examiners' conference, teachers may have different views on certain matters of detail or interpretation.

WJEC regrets that it cannot enter into any discussion or correspondence about this marking scheme.

WJEC GCSE MATHEMATICS – NUMERACY

AUTUMN 2023 MARKING SCHEME

GCSE Numeracy Unit 1: Intermediate Tier	Mark	Comments
$1(a) \frac{3}{10}$	B2	Mark final answer B1 for $\frac{15}{50}$ or $\frac{30}{100}$
1(b) 20 × 25 + 28 × 15 + 17 × 10 (= 500 + 420 + 170)	M2	M1 for either • sight of the sum of any 2 unique appropriate products (not multiples of these products) or • for sight of 20×25, 28×15 and 17×10
(£) 1090	A2	CAO. Answer space takes precedence FT from M2 or M1 to award A1 for either any 2 of 500, 420 and 170 in a correctly evaluated sum of 3 products or sight of 500, 420 and 170
		If no marks, award SC1 for sight of (Saturday and Sunday interchanged) 17 × 25 + 28 × 15 + 20 × 10 AND EITHER SC2 for an answer of (£)1045 OR SC1 for one of the following: any 2 of 425, 420 and 200 in a correctly evaluated sum of 3 products sight of 425, 420 and 200 award SC1 for sight of (table followed in order used in Venn) 20 × 25 + 17 × 15 + 28 × 10 AND EITHER SC2 for an answer of (£)1035 OR SC1 for one of the following: any 2 of 500, 255 and 280 in a correctly evaluated sum of 3 products sight of 500, 255 and 280

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2(a) <u>90</u> × 540 or ½ × 540 or 540 ÷ 4 or equivalent 360	M1	
135 (people)	A1	Answer space takes precedence
		When repeatedly halving 540, if there are errors, award M0 A0 unless indication that the intention is to divide by 2, e.g. • 540 ÷ 2 = 220 (error), 220 ÷ 2 = 110 is M1 A0 • 540, 220, 110 is M0 A0
2(b) Angle measured 170(°) ± 2(°)	B1	May be seen on the pie chart
0.4 × 170(° ± 2°) or equivalent	M1	FT for 'their angle, provided 90° < 'their angle' < 180° Any method of repeated addition must clearly be addition to 40%
68(°) or angle in the range 67(°) to 69 (°)	A1	Only allow angles in this range provided not from incorrect working Answer space takes precedence Allow A1 for labelled angle on the pie chart if no final answer given. On FT, using 'their 170', allow angles correctly rounded or truncated to the nearest degree
$2(c) 540 - \frac{7}{10} \times 540 \text{ or } (1 - \frac{7}{10}) \times 540 \text{ or } \frac{3}{10} \times 540$	M1	For complete method
162 (not children)	A1	Answer space takes precedence
		If no marks, award SC1 for sight of $(\frac{7}{10} \times 540 =) 378$

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$3(a)(i) (1 \times i)$ $\frac{10}{4} \times 1000 \text{ or } 1000 \times 10 \div 4 \text{ or } 1000 \times 2.5$ or equivalent	M2	M1 for appropriate sight (that need not be within a product) of any one of the following: • 2.5 (may be seen in the answer space) • $\frac{10}{4}$ • 10 ÷ 4 • (1 litre =)1000 (cm ³) • sight of digits 25 with incorrect place value
2500 (cm ³)	A1	CAO. Answer space takes precedence
3(a)(ii) 2.4 (kg)	B2	Answer space takes precedence B1 for any one of the following: attempt to multiply 200 by 12 which may include a place value error, or equivalent shown as repeated addition, e.g. 2 × 12, 20 × 12, 2000 × 12, sight of 2400 in working an answer of 2400 48/4 × 200 2kg 400g
3(a)(iii) 1:8:2	B2	Answer space takes precedence If units (g) are included then B1 only. B1 for sight of any one of the following (ignoring inclusion of 'g'): 25:200:50 5:40:10 equivalent multiple of the ratio 1:8:2 a ratio involving 1, 8 and 2 in an incorrect order
3(a)(iv) Sight of a suitable division, e.g. • 400 ÷ 28 • 400 ÷ 25 • 400 ÷ 30	M1	Allow if written a s a fraction rather than as a division
• 390 ÷ 30 Answer in the range 13 to 16	A1	Must be from sight or attempt at a suitable division or unsupported Allow an answer in the range from sight of repeated addition or multiplication (that may include rounding within additions)
3(b)(i) 6 g	B1	
3(b)(ii) (Daily recommendation =) 0.8 × 70	M1	Allow if embedded in further incorrect working only if this working includes the use of '14'
56 (g)	A1	Ignore any incorrect unit given, e.g. % or kg
25 (%)	A2	FT 14 for possible A2 or A1 'their 0.8 × 70' On FT allow rounding or truncation of the final percentage A1 for one of the following: • the fraction 14/56 or 7/28 or 1/4 • a clear full method finding percentages of 56(g) clearly working towards 14(g)

4(a)		Ignore \$ written as £ or €, etc
$(\frac{1}{5}$ is \$40, total amount of gift is) 40×5 or $40 \div \frac{1}{5}$	M1	ignore \$ minor as 2 or 6, ore
(\$)200	A1	ISW
(Amount gifted to animal charity is ½ × 200) (\$)50	B1	FT ¼ × 'their 200' correctly evaluated, provided • 'their 200' ≠ 40 • 'their 200' ≠ 200 – 40 (= 160) Allow FT 'their 200' = 8 (see note below)
(Gift to medical research is) (\$) 200 – 40 – 50	M1	FT 'their derived 200' – 40 – 'their 50', provided > 0
(\$) 110	A1	FT provided both M marks previously awarded
		If no marks, award SC1 for $(40 - \frac{1}{5} \times 40 - \frac{1}{4} \times 40 = 40 - 8 - 10 =)$ (\$)22
4(a) <u>Alternative method</u> (Total amount of gift is) 40×5 or $40 \div \frac{1}{5}$	M1	Ignore \$ written as £ or €, etc
(\$)200	A1	ISW
(Proportion given to medical charity) $ (1 - \frac{1}{5} - \frac{1}{4} =) \qquad \frac{11}{20} $ or $(1 - 0.2 - 0.25 =) \qquad 0.55$ or $(100 - 20 - 25 =) \qquad 55$ (%)	B1	Allow for proportion given to children's and animal charity clearly shown as $\frac{9}{20}$, 0.45 or 45 (%)
(Gift to medical research is) $\frac{11}{20} \times 200$ or $200 - \frac{9}{20} \times 200$	M1	FT 'their incorrectly evaluated $1 - \frac{1}{5} - \frac{1}{4}$ ' or 'their incorrectly evaluated $\frac{1}{5} + \frac{1}{4}$ as appropriate and 'their derived 200', provided • 'their $200' \neq 40$ • 'their $200' \neq 200 - 40$ (= 160) Allow FT 'their $200' = 8$
(\$) 110	A1	FT provided both M marks previously awarded
4(a) Organisation and communication	OC1	For OC1, candidates will be expected to: • present their response in a structured way • explain to the reader what they are doing at each step of their response • lay out their explanations and working in a way that is clear and logical • write a conclusion that draws together their results and explains what their answer means
Writing	W1	For W1, candidates will be expected to: • show all their working • make few, if any, errors in spelling, punctuation and grammar • use correct mathematical form in their working • use appropriate terminology, units, etc.

4(b) Sight of 30 000 – 10 000 or 20 000	B1	Ignore incorrect units given throughout
(30 000 - 10 000) × 0.22 or 20 000 × 0.22 or equivalent	M1	Any repeated addition method of 10% and 1% must clearly show addition to 22%
(\$) 4400	A1	CAO. Mark final answer
5(a) 209° ± 2°	B1	Answer space takes precedence
5(b)(i) Answer in the range 21 (km) to 25 (km)	B1	Answer space takes precedence
5(b)(ii) Correct interpretation of the map scale, e.g. 1 cm represents 25 000 cm or 250 m 2 cm represents 50 000 cm or 500 m or 0.5 km 4 cm represents 100 000 cm or 1 000 m or 1 km OR Correct conversion 12 km to cm, 25 000 cm to km or equivalent, e.g. (12 km =) 1 200 000 (cm) (25 000 cm =) 0.25 (km) sight of 12 and 0.25	B1	
12 ÷ 0.25 or 12 × 4 or 1200 000 ÷ 25 000 or 1200 ÷ 25 or equivalent	M1	Ignore place value error, e.g. 12 ÷ 'their number with digits 25', 12 × 'their number with digit 4'
48 (cm)	A1	CAO
5(b)(ii) <u>Alternative method</u> (Original map scale is 3 cm : 12 km =) 3 : 1 200 000 or 1 : 400 000 or equivalent	B1	
$\frac{400\ 000}{25\ 000} \times 3$ or 16×3 or equivalent 48 (cm)	M1 A1	Ignore errors in place value CAO

6(a)(i) Correct statement of Pythagoras' theorem • (Height² =) 50² – (60 ÷ 2)² • (Height² =) 50² – 30² • 50² = height² + (60 ÷ 2)² • 50² = height² + 30²	M1	Clear indication that all measurements have been converted to 3cm, 5cm, 4cm may be awarded all marks
Correct stage of evaluation • (Height ² =) 2500 – 900 • (Height ² =) 1600 • sight of $\sqrt{1600}$ • (Height =) $\sqrt{(50^2 - 30^2)}$	A1	Working must be seen Allow M1 A1 for a slip in the initial notation then corrected at this evaluation stage
(Height =) $\sqrt{1600}$ (Height = 40 mm) or Height² = 1600 (Height = 40 mm) or 1600 = 40² (Height = 40 mm)	A1	Mark final answer A0 for an incorrect statement, e.g. $\sqrt{1600} = 40^2$
6(a)(i) Alternative method 1 Identifies the relationship '3, 4, 5' and relates to the given (right-angled) triangle, e.g. sight of 3, 4, 5 and 30(mm), 40(mm), 50(mm) 3cm, 4cm, 5cm 3, 4, 5 and '× 10' 30, 40, 50 and '÷ 10' AND a statement or conclusion, e.g. Pythagorean triple Right-angled triangle 3, 4, 5 triangle means it would be 30, 40, 50 triangle	B3	For B3 there mus t be an accompanying statement or conclusion B2 for identifying the relationship '3, 4, 5' and relates to the given(right-angled) triangle • without a conclusion or statement, or • with an incorrect conclusion or statement B1 for sight of any one of the following: • '3, 4, 5' • 30 (mm) and 40 (mm) appropriately indicated on the diagram • A right-angled triangle drawn (with or without 90° indicated) appropriately labelled 30 (mm), 40 (mm) and 50 (mm)
6(a)(i) Alternative method 2 Assuming height as 40mm with use of 50mm or 30mm within a correct statement of Pythagoras' Theorem, e.g. • ((½ base)² =) 50² – 40² • 50² = 40² + x² • ((hypotenuse)² =) 40² + 30²	M1	Clear indication that all measurements have been converted to 3cm, 5cm, 4cm may be awarded all marks
Correct stage of evaluation, e.g. • $((\frac{1}{2} \text{ base})^2 = 50^2 - 40^2 =) 900$ • $(\frac{1}{2} \text{ base} =) \sqrt{900}$ • $((\text{hypotenuse})^2 = 40^2 + 30^2 =) 2500$ • $(\text{hypotenuse} =) (\frac{1}{2} \text{ base} =) \sqrt{2500}$	A1	Working must be seen
Appropriate full evaluation, e.g. • (½ base =) 30 (mm) • (hypotenuse =) 50 (mm)	A1	Mark final answer
6(a)(ii) (Volume) ½ × 60 × 40 × 20 or equivalent	M2	M1 for sight of area of X-section possibly in stages, $\frac{1}{2} \times 60 \times 40$ or $\frac{1}{2} \times 30 \times 40 + \frac{1}{2} \times 30 \times 40$ (= 1200 mm ²)
24 000 (mm³) (> 20 000 mm³)	A1	CAO

6(b) Sight of or implication that: 5 × number of people + 105 = 207 + 3 × number of people or 5x + 105 = 207 + 3x	M1	Implication includes attempt to balance costing for the same number of people ≥ 3 at each venue, e.g. • (10 people) 5 × 10 + 105 with 207 + 3 × 10 • (110, 115,) 120 with (210, 213,) 216
(5 – 3) × number of people = $207 - 105$ or number of people = $\frac{207 - 105}{5 - 3}$ or $5x - 3x = 207 - 105$ or $2x = 102$	m1	Includes correctly evaluated trial to attempt to balance costing for the same number of people at each venue provided 'their trial for 30 ≤ the number of people ≤ 70', e.g. correct costing for both venues for 40 people as (FH) (£)305 and (ML) (£)327 From M1, allow 1 slip in the rearrangement of 'their equation' provided 'their equation' is then simplified to
51 (people)	A1	ax = b, where a \neq 0 and b \neq 0 Sight of cost (£)360 for each venue implies M1 m1 CAO If no marks, award SC1 for finding the number of (whole) people for the same cost at each venue, provided the cost is > (£) 220
7. $ (4(.)40 \div 3.3) \times 9 \div 10 \qquad \qquad (= \frac{4(00)}{3} \times \frac{9}{10}) $ or $ (\frac{9}{10} \times 4(.)40) \div 3.3 \qquad \qquad (= \frac{3.96}{3.3}) $ or $ 4 \times \frac{9}{10} \div 3 \qquad \qquad (= \frac{3.60}{3}) $ or equivalent full method	M2	Accept equivalent in pence throughout M1 for any one of the following or equivalent: • (1kg Sparkle costs) $4(.)40 \div 3.3 = (=\frac{4(00)}{3})$ • (3.3kg Dazzle costs) $\frac{9}{10} \times 4(.)40 = (=3(.)96)$ • (3kg Dazzle costs) $4 \times \frac{9}{10} = (=3(.)60)$ • (3kg Sparkle costs) $4(.)00$
(£)1.2(0) or 120(p)	A2	CAO. If units are given they must be correct Do not award A2 or A1 from incorrect working Award A1 (from M1 or M2) for any one of the following: • (1kg Sparkle costs) $\frac{4(00)}{3}$ or 1.33() or 133.() • (3.3kg Dazzle costs) 3(.)96 • (3kg Dazzle costs) 3(.)60 Award A1 (from M2) for a correctly evaluated FT, with final answer rounded or truncated to a penny, for any one of the following: • 'their $4(.)40 \div 3.3' \times \frac{9}{10}$ • 'their $\frac{9}{10} \times 4(.)40' \div 3.3$ • 'their $4 \times \frac{9}{10}$ ' $\div 3$

8(a)(i) (2.5, 42) stated with a suitable line of best fit drawn through this point	B2	For B2 do not ignore the answer space stating an incorrect point, or giving reverse coordinates Conditions of a suitable line of best fit: The straight line (accept intention if a ruler is not used) must have points above and below it The line must be of sufficient length, to illustrate trend for at least 6 points The trend shows that there are points above and below the line towards each end of the line For B2 the point (2.5, 42) must be stated or plotted with a suitable line of best fit through this point. If (2.5, 42) is not stated or plotted, then it is only possible to award a maximum of B1 Allow B2 for one of the following: a blank answer space with (2.5, 42) plotted with a suitable line of best fit through (2.5, 42) (2.5, 42) stated in the answer space, but not plotted, with suitable line of best fit passing through (2.5, 42) B1 for sight of any one of the following: (2.5, 42) stated in the answer space blank answer space with (2.5, 42) indicated by a correct plot A suitable line of best fit for the given points: with no additional point plotted passing through 'their additional incorrect point' (plotted) suitable if 'their additional incorrect point' plotted is ignored
8(a)(ii) Reading from line of best fit for number of cups (tolerance to the nearest gridline) for rainfall of 2.0 mm	B1	Answer space takes precedence STRICT FT from (a)(i) 'their line of best fit' which must be drawn for negative correlation No mark is awarded if no line of best fit drawn in (a)(i)
8(b) 5 × 18 + 5 × 0.5 or 18.5 × 5 92.5 (cm)	M1 A1	Allow for 18 < 'their 18.5' ≤ 19 CAO
		If no marks, award SC1 for sight of 18.5 (cm) or 18.4999(cm) provided clearly a recurring 9 digit
8(c) Selects or unambiguously implies 'No' with a reason, e.g. '(Space) minimum 97.25 (cm) (which is less than 97.3 cm)'	E1	Allow 'No' with a reason, e.g. '97.25 (cm)' '(least) 97.25 and (greatest) 97.75' Do not accept 'No' with the reason, e.g. '97.75 (cm)'

9(a)(i) Entries 146 and 160 in the table and the cumulative frequency diagram completed correctly (correct plots (11, 146) and (13, 160) and all plots joined)	B2	 B1 for any one of the following: 146 and 160 in the table, correct plots but not joined 146 and 160 in the table, with one correct plot and one incorrect plot in completing the cumulative frequency diagram with plots joined one error in the table, including FT 'their 146' + 14 and these cumulative entries used correctly to complete the cumulative frequency diagram with plots joined correct cumulative frequency diagram with plots joined, with incorrect, incomplete or not attempted entries in the table
9(a)(ii) 8.2 to 8.4 (minutes)	B1	Answer space takes precedence Allow 8 minutes 12 seconds to 8 minutes 24 seconds FT reading from the graph for 'their median', from ½ × 'their 160', provided 'their 160' ≥ 110, with a tolerance of ½ small square from 'their <u>cumulative</u> frequency graph', provided it is possible to read 'their median' from the vertical axis on the graph paper provided
9(a)(iii) 7.2 minutes	B1	Answer space in the statement takes precedence, if blank award for indication of '7.2' (circled) in the list Allow '7' in the answer space provided 7.2 indicated in the list Do not accept '8' in the answer space if 7.2 indicated in the list
9(a)(iv) $\frac{20}{160}$ (× 100) or $\frac{1}{2}$ × 25 (%) or equivalent	M1	FT for (100 ×) 20/'their 160', provided 'their 160'> 106
12.5 (%) or 12½ (%)	A1	On FT allow rounding or truncation to 1 decimal place
9(b) (Costs are 180 + 220) (£) 400 AND (Profit is 700 – 180 – 220) (£) 300 OR (Receipts / Costs =) $\frac{700}{400}$ (× 100)	B1	May be embedded, e.g. 700 – 400 = 300 (= 1.75 or 175%)
(Percentage profit is) $\frac{300}{400}$ (× 100) or $\frac{700}{400}$ (× 100) - 1 (× 100)	M1	FT 'their 400' and 700 – 'their 400' provided their costs or profit are ≠ 180, ≠ 220 and ≠ 700
75 (%)	A1	CAO
		Allow if all costs and the total are consistently multiplied by 3.
9(c) 8(.)40 ÷ 1(.)20 or 8(.)40 – 8(.)40 ÷ 6 or equivalent	M1	Accept a complete and convincing method of trial and improvement
(£) 7 or 700 (p)	A1	If units are given they must be correct
		Sight of 7 + 1.40 = 8.40 is awarded M1 A0 unless (£)7 is selected

10(a)(i) King Edward and 90(g)	B1	
10(a)(ii) (90 – 52 =) 38(g)	B2	Do not award from sight of any incorrect working B1 for sight of any of the following: 52 and 90 Sight of 90 and 50 < 'their lowest mass' ≤ 54 and 90 − 'their lowest mass' correctly evaluated Answer of 35(g) and unambiguous selection of (King Edward) 98 and 63 or (Desiree) 88 and 53
10(b) Selects: Desiree, and Interquartile range and less than for the other 2 varieties	E1	
11. (Width of poster) 2 × $\frac{26.4}{2.4}$ or 2 × 11 or equivalent	M1	
22 (cm)	A1	Mark final answer for the width of the poster
(Perimeter of poster 2 × (22 + 26.4) =) 96.8 (cm)	A1	FT 'their 22' provided M1 previously awarded
100 (cm)	B1	FT provided 95 < 'their 96.8' <100, as 100 correct to 1 significant figure
		Accept working in mm or m, units must then be given in the final answer
		Do not accept an unsupported answer of 100 (cm)
11. <u>Alternative method</u> (Perimeter of stamp) 8.8 (cm) AND sight of $\frac{26.4}{2.4}$ (= 11) or $\frac{2.4}{26.4}$ (= $\frac{1}{11}$)	B1	
(Perimeter of poster) $ (2 + 2.4 + 2 + 2.4) \times \frac{26.4}{2.4} $	M1	FT 'their 2 + 2.4 + 2 + 2.4'
96.8 (cm)	A1	
100 (cm)	B1	FT provided 95 < 'their 96.8' <100, as 100 correct to 1 significant figure
		Accept working in mm or m, units must then be given in the final answer
		Do not accept an unsupported answer of 100 (cm)